Volume 35, No. 2 April 2025 Print ISSN 1229-3067 Online ISSN 2508-7908

# ADVANCED STUDFES FN CONTEMPORARY MATHEMATFCS

Memoirs of the Jangjeon Mathematical Society

Jangjeon Research Institute for Mathematical Sciences & Physics, Daegu, Korea

(章田數學會 記念論文集)

## ADVANCED STUDJES IN CONTEMPORARY MATHEMATICS

Memoirs of the Jangjeon Mathematical Society

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#### Print ISSN 1229-3067 / Online ISSN 2508-7908

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